

Logistics Solutions' Choice and Optimization in Emergency Conditions

Liu Tongjuan^{1,a}, Duan Yanlin^{2,b}, Jiang Rongfen^{2,c}

¹Information School, Beijing Wuzi University, 1 Fuhe Street, Tong Zhou District, Beijing, China, 101149; PH (86) 15210912868; email: ltj7905@163.com

²Graduate School, Beijing Wuzi University, 1 Fuhe Street, Tong Zhou District, Beijing, China, 101149;

a: ltj7905@163.com, b: duanyanlin@163.com, c: 18811177269@163.com

Abstract: In this paper, emergency logistics plan is studied by using the integrated knowledge of logistics operation management and operational research. According to the concept of emergency logistics and logistics application and development at home and abroad, combined with practical application of emergency logistics in emergency public events, Selection and optimization of logistics scheme are studied by using the analytic hierarchy process (AHP) and data envelopment analysis (DEA) methods under the condition of emergency.

Keywords: Emergency logistics; Analytic hierarchy process; DEA theory analysis; Scheme selection

INTRODUCTION

Emergency logistics means to provide the unexpected natural disasters, public health emergencies and other unexpected events for the purpose of emergency supplies needed to pursue maximum profit and losses of time minimizing the target of special logistics activities(Wei-lin Liu,2013). It has a sudden, uncertainty, unconventional, and the weak economy and other characteristics. In the unexpected event occurs, many plan to quickly select from one of the best programs in emergency logistics is an extremely important aspect. Therefore, this application of operations research by studying the level of analysis and gray theory method, an enterprise logistics solutions under emergency conditions to make the best choice to pursue to maximize the benefits of time and the goal of minimizing losses (Juan Wang,2015).

Analytical Hierarchy Process (AHP) is presented by the T.L.Saaty, in the 70s of last century. Because of its decision-making in dealing with complex issues of practicality and effectiveness, AHP is soon widely used in various fields (Jinfeng Wang,2012). However, comparison matrix is established by using AHP, only a single target is compared without considering the linkages between indicators. Evaluation indexes of emergency logistics solutions, however, are not independent of each other, and their relations are unclear, but exist, In essence, it is a gray relationship. Therefore, the preplan evaluation system is considered as gray Grey System Theory is mainly for the system model uncertainty, incomplete information under the conduct of systematic association analysis, model construction, through system which not only considers

the relative weights of various evaluations index but consider the relationship between the indexes.

DEA is created by Charnes and Cooper in 1978. DEA is used to evaluate relative effectiveness of more input and more output "departments" or "units" by using mathematical programming model (called DEA effective).

Specifically, the DEA is the use of mathematical programming model of decision making units compared between relative efficiency, decision making units to make comments. DEA model is based on the theory of mathematical programming, such as linear programming and its dual theory. At the same time, the DEA can be regarded as a treatment of multiple input multiple output of multi-objective decision-making method, therefore, it is especially applicable to have multiple input multiple output of complex system(Alessandra Cozzolino,2012).

This article draws on logistics management and operations research content, integrated use of theory to study the emergency logistics solutions under the conditions of choice, according to the concept of the proposed emergency logistics as well as in domestic and international logistics field application and development, combined with emergency logistics public emergency in the practical application of AHP and gray theory method of emergency conditions, the selection of logistics solutions.

BASED ON AHP METHOD OF THE EMERGENCY MODEL OF LOGISTICS SOLUTIONS

AHP Method to Determine Weights of Indicators

AHP to solve problems of all kinds of problems should first construct a hierarchy of plans, in which each layer determines the relative importance of

weights based on the factors, and calculates the relative weights which are correspond with evaluation index system of target layer.

Index System and the Establishment of Hierarchy

Currently, the major program of emergency logistics should be considered in practical applications in order to obtain optimal solution. In order to make the analysis of emergency logistics system more comprehensive and scientific, this paper presents the following evaluation: ① logistics services, including punctuality, integrity and security; ② logistics costs, including material costs, transportation costs and social environmental costs.

According to the three evaluations above, emergency logistics programs evaluation model are shown as Figure 1.

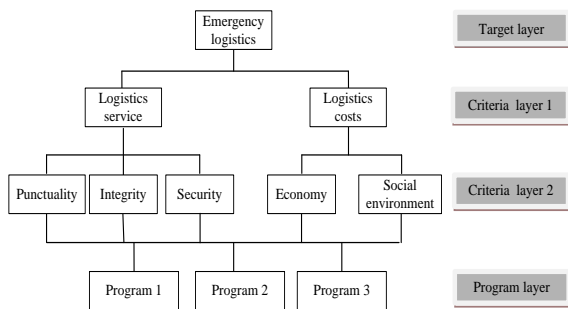


Figure 1. Emergency logistics program evaluation model

Structure Matrix

AHP proposed by Saaty scale from 1 to 9 of the comparison between the various factors are quantified comparison matrix, the matrix element values are compared the relative importance of the correspondence between the following: ratio of equal importance: $a_{ij} = 1, a_{ji} = 1$; A_i is a little more important than A_j ; $a_{ij} = 3, a_{ji} = 1/3$; A_i is obvious more important than A_j ; $a_{ij} = 5, a_{ji} = 1/5$; A_i is much more important than A_j ; $a_{ij} = 7, a_{ji} = 1/7$; A_i is extremely important than A_j ; $a_{ij} = 9, a_{ji} = 1/9$;

The weight Vector Calculation and Consistency Test

By using comparison matrix analysis, the weight values of each index are determined and the characteristic equation $AX = \lambda X$ of matrix A is judged, which λ is the Eigen value of A and X is the feature vector of A.

After normalization, the eigenvectors corresponding to the maximum Eigen value λ_{max} are the sorting weights which the same levels corresponding to a certain level factors have relative importance factor, denoted by the weight vector w . The w_i weight is the relative import degree of various factors. Commonly, the feature vector approximations are calculated by using the summation method.

1) Summation Method

For a consistent judgment matrix, its each column normalized is the corresponding weight vector. When A is inconsistent, each column normalized approximates weight vector. Summation method uses the n column vectors as the arithmetic average of the weight vector.

So,

$$w_i = \frac{1}{n} \sum_{j=1}^n \frac{a_{ij}}{\sum_{k=1}^n a_{kj}}, (i = 1, 2, 3, \dots, n)$$

The calculation steps of Summation Method are as follows: ① matrix elements of A normalized by the column; ② the normalized sum of each column; ③ will add up to get the vector divided by n weight vector.

2) Consistency check

To ensure the comparison result that we make non-contradictory and the result of AHP method meaningful, the need for consistency test.

First of all, calculating the consistency index CI,

$$CI = \frac{\lambda_{max} - n}{n - 1}$$

And, $\lambda_{max} = \frac{1}{n} \sum_{i=1}^n \frac{(AW)_i}{w_i}$

Then, calculated random coincidence rate CR,

$$CR = \frac{CI}{RI}$$

In the above formula, RI as the average random consistency index was the calculated average based on sufficient number of random samples of matrix consistency index. Values of RI are shown in Table 1.

Table 1. Values of RI

Order of Matrix	1	2	3	4	5	6	7	8	9
RI	0	0	0.52	0.89	1.12	1.26	136	1.41	1.46

The method of DEA

DEA is by Chames and Cooper who started in 1978 to create. DEA is the use of mathematical programming model evaluation is more input and more output "departments" or "units" (called the decision unit, Jian Ji for DMU) between the relative effectiveness (called DEA effective).

Its basic method is that treats every valued unit as a DMU, and the valued groups are made up of large numbers of DMU. Supposing that we have to value n DMU, and every DMU has m imports and s exports. including :

$$X_j = X_{1j}, X_{2j}, \dots, X_{mj}$$

$$Y_j = Y_{1j}, Y_{2j}, \dots, Y_{sj}$$

for every DMU $j, j \in \{1, 2, \dots, n\}$.

The C2R model which values the relative availability is as follows:

$$D\varepsilon \left[\begin{array}{l} \min [\theta - \varepsilon(e^T s^- + e^T s^+)] = V_{D\varepsilon} \\ S.t \sum_{j=1}^n X_j + S^- = \theta X_0 \\ \sum_{j=1}^n Y_j \lambda_j - S^+ = Y_0 \\ \lambda_j \geq 0, j = 1, 2, \dots, n \\ S^- \geq 0, S^+ \geq 0 \end{array} \right]$$

For $e^T = (1, 1, \dots, 1) \in E_m$, $e^T = (1, 1, \dots, 1) \in E_s$.

If the DEA (C2 R) model did not limit j , then this model belongs to CRS, and can be used to determine whether the system activities are effective from the aspect of technology and scale. if we introduced the constraint condition $j=1$, we would draw another BBC model of DEA, that is the VRS model, which can further judge the returns to scale state of systems activities. If $J=1$, then the DMU returns to scale is constant, if $j < 1$, means that the DMU returns to scale is increasing; $j > 1$, the DMU returns to scale is diminishing. When the calculation result of the model shows $\theta = 1$, and $S^- > 0, S^+ > 0$, the DMU is valid for DEA; $\theta \neq 1$, the DMU is invalid for the DEA.

The steps to determine the weight

Using the AHP method to determine weights

After we established the hierarchical structure, every indicator makes pair-wise comparison and builds judge according to the selected scale. By the given matrix we carry on the single-sort level and consistency checking. The single-sort level is necessary to calculate the relative importance of sorted weights of all the factors in the same level for the highest level, i.e. the level of total sort, this process are realized layer by layer from the highest to the lowest level. Finally we get the weights α_i ($i = 1, 2, \dots, n$).

The DEA to determine the weight

Establishing DEA model, we need to translate this model into the linear programming model which we can resort to the dual theory to solve this problem, and get the optimal efficiency evaluation index, finally we could get weights β_i ($i = 1, 2, \dots, n$).

Determining the weight by Combination method

Use the formula $\phi_i = \lambda \alpha_i + (1 - \lambda) \beta_i$, we can get the total combination weight.

PRACTICAL APPLICATIONS

A company needs to transport washing machines to its distributors peremptorily and formulate three emergency logistics plan. Experts gave the score of the three method based on the above six indicators.

AHP Method to Determine Weights of Indicators

With 1 to 9 scale method to construct the Matrix and the consistency test as follows:

Judgment matrix and calculation results of overall goal are shown as table 2.

Table 2. Judgment Matrix and Calculation Results of Overall Goal

A	B1	B2	Wi
B1	1	3	0.75
B2	1/3	1	0.25

Note: $\lambda_{max} = 2$, CI = 0, RI = 0, CR = 0 < 0.1

Judgments matrix and calculation results of B1, C1, C2, and C3 for logistics services are shown as table 3.

Table 3. Judgments Matrix and Calculation Results of B1, C1, C2, and C3 for Logistics Services

B1	C1	C2	C3	Wi
C1	1	1	5	0.4545
C2	1	1	5	0.4545
C3	1/5	1/5	1	0.0910

Note: $\lambda_{max} = 3.0423$, CI = 0.0236, RI = 0.52, CR = 0.0454 < 0.1

Judgment matrix and calculation results of B2, C4 and C5 for logistics costs are shown as table 4.

Table 4. Judgment Matrix and Calculation Results of B2, C4 and C5 for Logistics Costs

B2	C4	C5	Wi
C4	1	5	0.8333
C5	1/5	1	0.1667

Note: $\lambda_{max} = 2$, CI = 0, RI = 0, CR = 0 < 0.1

Judgments matrix and calculation results of C1, D1, D2, and D3 for logistics program are shown as table 5.

Table 5. Judgments Matrix and Calculation Results of C1, D1, D2, and D3 for Logistics Program

C1	D1	D2	D3	Wi
D1	1	3	5	0.6370
D2	1/3	1	3	0.2583
D3	1/5	1/3	1	0.1047

Note: $\lambda_{max} = 3.0523$, CI = 0.0324, RI = 0.52, CR = 0.0623 < 0.1

In the same logic, we can get Judgments matrix and calculation results of C, D1, D2, and D3 for logistics program in table 6.

Table 6. Judgments Matrix and Calculation Results of C, D1, D2, and D3 for Logistics Program

	C1	C2	C3	C4	C5	
Program	D1	0.633	0.088	0.429	0.656	0.143
	D2	0.261	0.243	0.429	0.187	0.143
	D3	0.106	0.669	0.143	0.158	0.714

Note: All the judgments matrix and calculation results are effective

So we can draw the conclusion in table 7.

Table 7. The Total Computation Results

Criteria layer 1	B1		B2		Total weight of program		
	0.75		0.25				
Criteria layer 2	C1	C2	C3	C4		C5	
		0.455	0.455	0.091	0.833	0.167	
Program level	D1	0.633	0.088	0.429	0.656	0.143	0.418
	D2	0.261	0.243	0.429	0.187	0.143	0.247

	D3	0.106	0.669	0.143	0.158	0.714	0.337
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From the table 7 we know that D1 is the best of three programs, so we choose the program D1.

DEA Method to Determine Weights of Indicators

The impact factor values of the program are shown

	Time (day)	Secu- rity	Damage rage(%)	Econo- mical costs	Social Environme- nt costs
Program 1	1	1	5	6	2
Program 2	2	1	7	6.5	1
Program 3	1.5	1	7	7	3

as table 8.

Table 8. The impact factor values of the program

The establishment of the DEA model

The three programs point to the decision unit DMU 1, DMU 2, and DMU 3.

For the decision unit DMU_j (j = 1, 2, 3), punctuality are regarded as output indicator 1, the safety index as output indicator 2, the damage rate as output indicator 3, the economic costs as output indicator 4, social environment costs as output indicators 5. We treat input indicators for the program, all the production unit input indicators are 1. So this problem can be translated into C2R model.

The Input and output value of decision units are shown as table 9.

Table 9. The Input and output value of decision units

	Output 1	Output 2	Output 3	Output 4	Output5	input
DMU1	1	1	5	6	2	1
DUM2	2	1	7	6.5	1	1
DUM3	1.5	1	7	7	3	1

$$\begin{aligned} \max \theta_1 &= \frac{u_1 + u_2 + 5u_3 + 6u_4 + 2u_5}{v} ; \\ s t \frac{u_1 + u_2 + 5u_3 + 6u_4 + 2u_5}{v} &\leq 1 ; \\ \frac{2u_1 + u_2 + 7u_3 + 6.5u_4 + u_5}{v} &\leq 1 ; \\ \frac{1.5u_1 + u_2 + 7u_3 + 7u_4 + 3u_5}{v} &\leq 1 ; \end{aligned}$$

We can solve the linear programming model by Lingo software, and find the optimal efficiency evaluation index $\theta_1=0.978$, Similarly we can obtain DMU2, $\theta_2=1.00$, DMU3 : $\theta_3=0.197$.

The Second step, to seek a combination of weight

Use the formula $\phi_i = \lambda \alpha_i + (1-\lambda)\beta_i$, in this paper, the method of DEA and AHP reflects that the objective and subjective preference of decision-makers is relatively modest, so they chose $\lambda = 0.5$, λ can be given based on personal preferences. The combined

weights of three options are calculated as follows:

$$\begin{aligned} \phi_1 &= \frac{0.418+0.979}{2} = 0.6985 \\ \phi_1 &= \frac{0.247+1.00}{2} = 0.6235 \\ \phi_2 &= \frac{0.337+0.197}{2} = 0.267 \end{aligned}$$

This shows that the value of program1 is the maximum, so the program is more reasonable.

CONCLUSIONS

This paper studies Emergency Logistics mechanism and emergency logistics system, treats qualitative and quantitative analysis as the guiding ideology, applies creatively DEA and AHP to the emergency logistics solutions selection. By Introducing gray correlation analysis, we can overcome defects which various indicators are independent when we use the Analytic Hierarchy Process between, the combination of AHP and DEA method not only takes the subjective indicators weight into account, also applies the weight of objective indicators, makes the evaluation process free of subjective factors to some extent, and the workload e is reduced.

By studying emergency logistics examples, we can prove that the combination of AHP and DEA method is valuable in solving the practical emergency logistics solutions problems.

In this paper, we can not only enhance the accuracy of the program, and also provide a new method for the choice of logistics solutions under emergency conditions.

ACKNOWLEDGMENT

This work was supported by funding project for Youth Talent Cultivation Plan of Beijing City University Under the grant number (CIT&TCD201504051) and this work was supported by Beijing Wuzi University Cultivation Fund Project (GJB20143006) .

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